

Saturday Math: Elementary to Middle

A closer look at proportional reasoning through the grades.

Norms

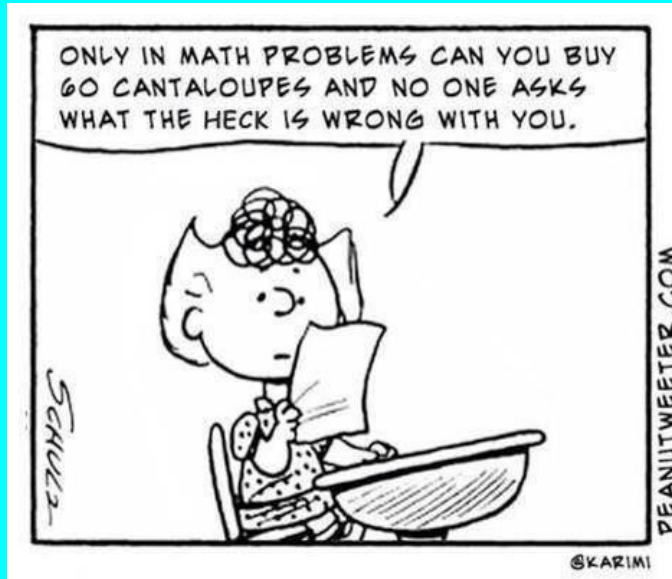
- We take care of our own needs while recognizing our responsibility to the group.
- We listen with the intent to understand; we speak with the intent to contribute.
- We treat disagreement as a positive opportunity for learning.
- We are respectful and mindful of our own and others' strengths, challenges, and learning styles.
- We promote a collaborative, generative, and reflective environment.

Focus Questions of the Day

What is the mathematical story of proportional reasoning across elementary and middle school mathematics?



What is proportional reasoning?



What is a Strand Trace?

We will **Explore the Mathematics** of some rich tasks from K-8.

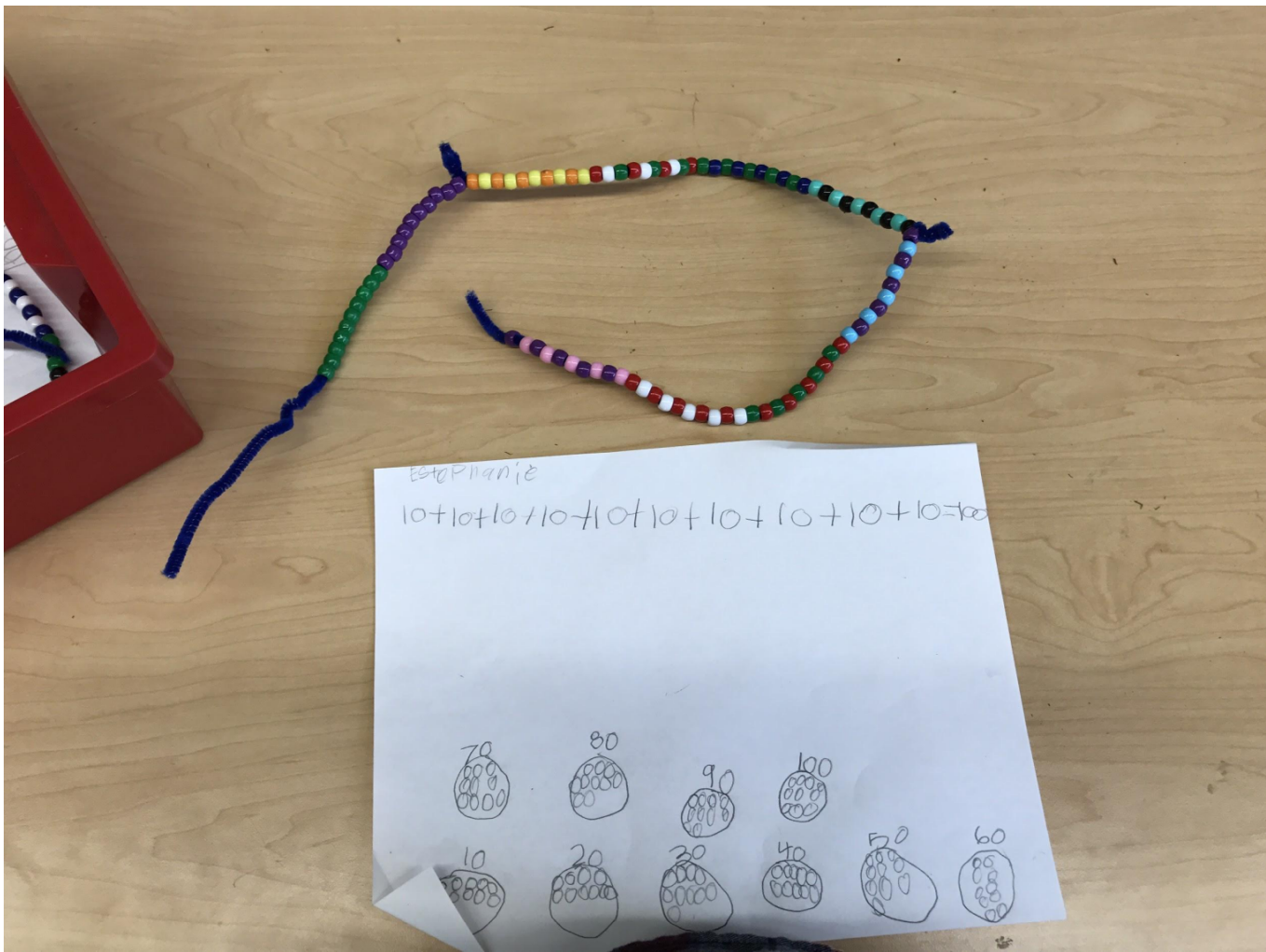
Examine the **connections** between the explicit and underlying mathematical concepts from each task.



Kindergarten/First Grade Structuring: Place Value

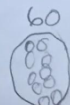
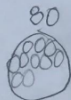
To celebrate the hundredth day of school, we are going to make bead necklaces with *exactly 100 beads*.

Make a plan and then follow your plan.



Estimación

$$10+10+10+10+10+10+10+10+10+10=100$$



Atgalo

Yo voy a contar eh lo eh lo

10 10 + 10 + 10 + 10 + 10 + 10 + 10 + 10 + 10 + 10

10

20

30

40

50

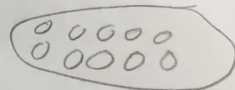
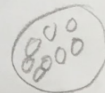
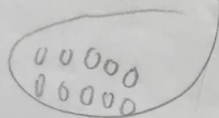
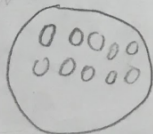
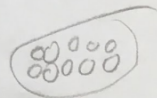
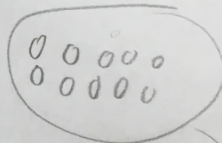
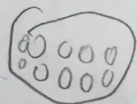
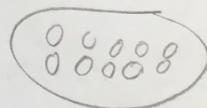
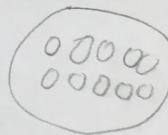
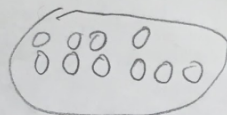
60

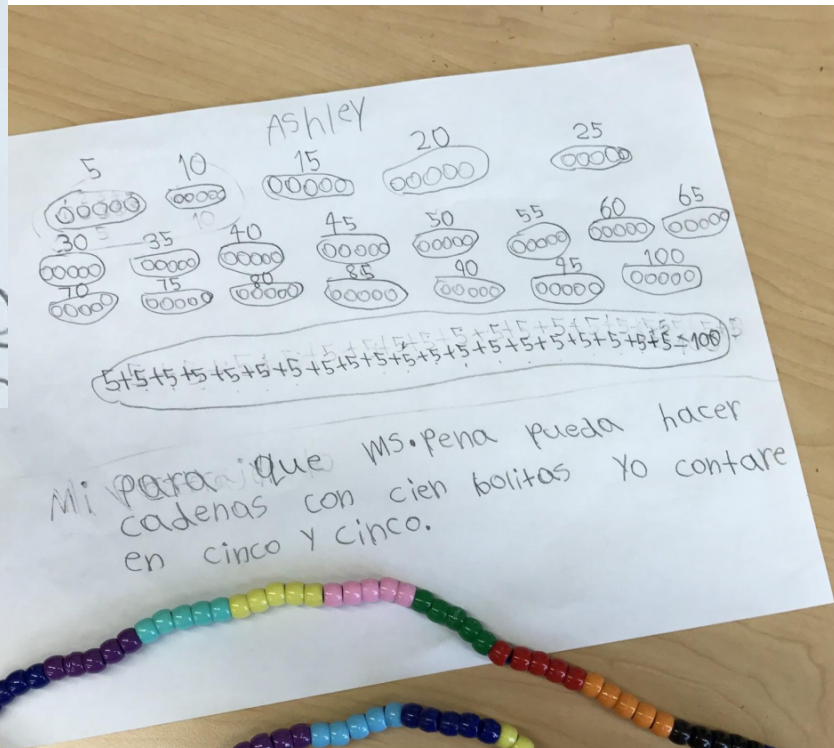
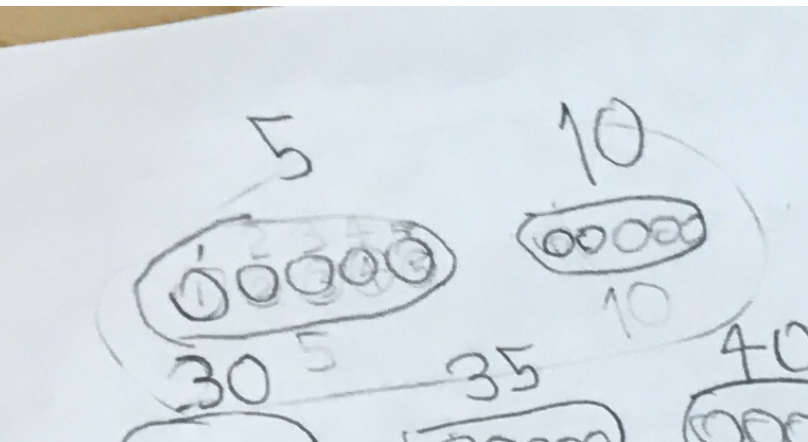
70

80

90

100



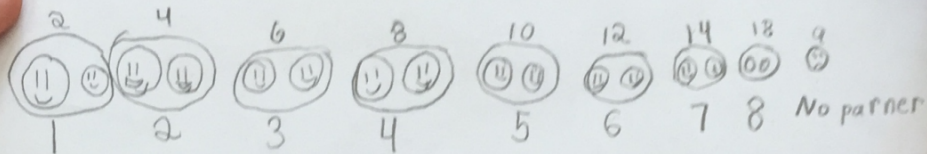


1st Grade Structuring: Properties of Number

We have 24 kids in our class. When we play math games, will everyone have a partner?

Melania

3

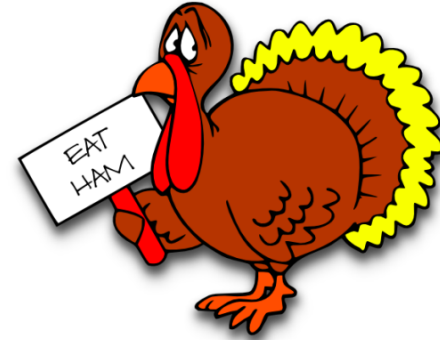


8 partnerships

1 partnership is
a lone only 1 person
is in it.

each partnership has
two in side it.
they are like doublets like
1 partnership is equal
to 1+1=2.

3rd Grade: Turkey Problem



What a Big Dinner!

\$1.25

What do you notice about \$1.25?



* 5 quarters is equal to \$1.25.

* 12 dimes and one nickel equals \$1.25.

* If you multiply \$1.25 by 4, you get \$5.

$$4 \times \$1 = \$4 \quad \text{and} \quad 4 \times \$0.25 = \$1$$
$$\$4 + \$1 = \$5$$

* \$1.25 is 125 cents.

→ 100 + 25 ←

* The decimal point separates the dollar from the cents.

\$1 and 25¢

Stanley's prediction:

Every time you multiply \$1.25 by a multiple of 4, the product will always be a multiple of 5.

Turkey problem

$11b = 1.25 \quad 29 \text{ pounds}$

$$\begin{array}{r} 24 \times 25 \\ \underline{24} \\ 600 \end{array}$$

[illegible]

$$\frac{21}{1} \times \frac{5}{4} = \frac{120}{4}$$

The Turkey problem

Part I

1.25 per lb
24 lb How much does it cost?

Part II

15 mins per lb
How long will it take to cook?

The turkey problem

Part I

\$ 1.25 per lb
24 lb

How much does it cost?

1.25 x 4 = \$5.00
1.25 x 4 = \$5.00
1.25 x 4 = \$5.00
1.25 x 4 = \$5.00
1.25 x 4 = \$5.00
1.25 x 4 = \$5.00
the \$30.00

five
four
are the
20.

The Turkey Problem

Part I

Work

How much money
does it cost? 30

$$\begin{array}{cccc} 1 & 2 & 3 & 4 \\ 25 & + 25 & + 25 & + 25 = 100 \end{array}$$

$$\begin{array}{cccc} 5 & 6 & 7 & 8 \\ 25 & + 25 & + 25 & + 25 = 100 \end{array}$$

$$\begin{array}{cccc} 9 & 10 & 11 & 12 \\ 25 & + 25 & + 25 & + 25 = 100 \end{array} \quad 300 + 300 = 600$$

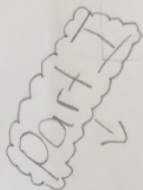
$$12 + 12 = 24$$

$$24 \times 1 = 24$$

$$24 + 6 = \boxed{30\$} \text{ answer}$$

The turkey problem

Name: Maribel
Date: 1/3/17



$$600 = 6.00 \$$$

$$\begin{array}{r} 6.00 \\ + 24.00 \\ \hline \text{Answer: } 30.00 \end{array}$$

dubble the 15

$$\begin{array}{r} 3 \times 5 = 15 \\ 3 \times 5 = 15 \\ \hline 30 \end{array}$$

Part 1: \$1.25 per LB

24 LB

$$\begin{array}{r} 25 \\ \times 24 \\ \hline 100 \\ 500 \\ \hline 600 \end{array}$$

$$\begin{array}{r} 24 \\ + 6 \\ \hline \$30 \end{array}$$

12 LB = \$5

$$\begin{array}{r} 15 \\ + 15 \\ \hline \$30 \end{array}$$

24 LB = total

Key:

$$\begin{array}{l} 24 - 4 = 20 \\ 20 - 4 = 16 \\ 16 - 4 = 12 \\ 12 - 4 = 8 \\ 8 - 4 = 4 \\ 4 - 4 = 0 \end{array}$$

4 quarters = \$1.00

The Turkey Problem

24 LB

\$1.25 is \$25
The decimal
point separates
the dollar from
the cent

$$\begin{array}{r} 20 \\ 400 \\ 100 \\ \hline 600 \end{array}$$

Provided

$$\begin{array}{r} 20 \\ 400 \\ 100 \\ \hline 600 \end{array}$$

$$\begin{array}{r} 15 \\ + 15 \\ \hline 30 \end{array}$$

$$\begin{array}{r} 25 \\ \times 24 \\ \hline 600 \end{array}$$

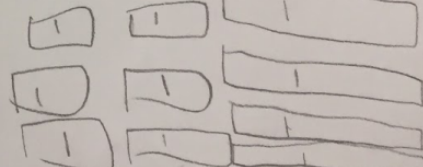
600 cents is \$6.00

$$\begin{array}{r} \$24.00 \\ + \$6.00 \\ \hline \end{array}$$

$$\begin{array}{r} \$30.00 \end{array}$$

$$\begin{array}{r} 100 \\ + 100 \\ + 100 \\ + 100 \\ + 100 \\ \hline 600 \end{array}$$

\$1.25 is \$125



Turkey Problem

part 1 \$1.25 per lb
24 lb

How much does it cost?

Double it.

1.25 x 20 = 25.00
1.25 x 4 = 5.00
25.00 + 5.00 = 30.00

36 Double it.
1.25 x 20 = 25.00
1.25 x 10 = 12.50
1.25 x 5 = 6.25
25.00 + 12.50 + 6.25 = 43.75

NSWR: 30.00

The Turkey

stanley

24
x 1

24

Part 1 The turkey problem

I bought 24 pounds

\$ 30.00

Square = $\frac{S}{4}$

$$\begin{array}{r} 24 \\ 125 \\ 125 \\ 125 \\ 125 \\ 125 \\ 125 \\ 125 \\ + 125 \\ \hline 1000 \\ 1000 \\ 1000 \\ + \\ \hline 3000 \end{array}$$
$$3^{10s} \times 8^{10s} = 24 \text{ lbs}$$

The Turkey Problem

Stanley

$$\begin{array}{r} 24 \\ \times 1 \\ \hline 24 \end{array} \text{ \$}$$
$$\begin{array}{r} 24 \\ \times 25 \\ \hline 600 \\ 480 \\ \hline 600 \end{array}$$

600¢ = 6.00

Answer, $\begin{array}{r} 24.00 \\ + 6.00 \\ \hline 30.00 \end{array} \text{ \$}$

~~$$\begin{array}{r} 24 \\ \div 2 \\ \hline 12 \\ \times 5 \\ \hline 60 \end{array}$$~~

Stanley

$$\begin{array}{r} 24 \\ \times 1 \\ \hline 24 \$ \end{array}$$
$$\begin{array}{r} 24 \\ \times 25 \\ \hline 120 \\ + 480 \\ \hline 600 \end{array}$$
$$600 \text{¢} = 6.00$$
$$\begin{array}{r} 24.00 \\ + 6.00 \\ \hline 30.00 \end{array}$$

Answer, 30.00 \$

$$\begin{array}{r} 24 \\ 2 \overline{) 48} \\ \underline{48} \\ 0 \end{array}$$

7th Grade: Gym Memberships

Do the Math!

Resources: Lab-sheet, Graph Paper, Colored Pencils, Straight Edge

Think About: What is the math? How have we seen it come up during the day in other grades?



7th Grade: Gym Member



In January, Georgia signed up for a membership at Anytime Fitness. The plan she chose cost \$95 in start-up fees and then \$20 per month starting in February. Edwin also signed up at Anytime Fitness in January. His plan cost \$35 per month starting in February, and his start-up fees were waived.

Who got the better deal? How do you know?

- Resources Available:
Graph Paper, Colored Pencils, Sticks, Blank
Tables

Connections
?

Reflection & Closing

Reflection form

One Word that describes your learning experience of the morning.

